# Package: msd (via r-universe)

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|--|
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| Imports stats  |
| <b>Description</b> Implements the method of successive dichotomizations by Bradley and Massof (2018) <doi:10.1371 journal.pone.0206106="">, which estimates item measures, person measures and ordered rating category thresholds given ordinal rating scale data.</doi:10.1371> |
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| expdata | Expected Ratings Matrix |  |
|---------|-------------------------|--|
|         |                         |  |

# **Description**

Expected ratings matrix given item measures, person measures and ordered rating category thresholds.

# Usage

```
expdata(items, persons, thresholds, minRating)
```

# Arguments

| items      | a numeric vector of item measures with missing values set to NA.         |
|------------|--|
| persons    | a numeric vector of person measures with missing values set to NA.       |
| thresholds | a numeric vector of ordered rating category thresholds with no NA.       |
| minRating  | integer representing the smallest ordinal rating category (see Details). |

# **Details**

It is assumed that the set of ordinal rating categories consists of all integers from the lowest rating category specified by minRating to the highest rating category, which is minRating + length(thresholds).

#### Value

A numeric matrix of expected ratings.

# Note

Expected ratings are literally the expected value of the ordinal rating categories when treated as integers. Expected ratings that cannot be calculated return as NA (e.g., if either the person or item measure is NA). Intended use is for chi-squared tests or for calculating infit and outfit statistics.

## Author(s)

Chris Bradley (cbradley05@gmail.com)

#### See Also

misfit

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# **Examples**

```
# Using randomly generated values with minimum rating set to zero
im < -runif(20, -2, 2)
pm < -runif(50, -2, 2)
th \leftarrow sort(runif(5, -2, 2))
m <- expdata(items = im, persons = pm, thresholds = th, minRating = 0)
```

ims

Item Measures

# **Description**

Estimates item measures assuming person measures are known and all persons use the same set of rating category thresholds.

## Usage

```
ims(data, persons, thresholds, misfit = FALSE, minRating = NULL)
```

# **Arguments**

| data    | a numeric matrix of ordinal rating scale data whose entries are integers with missing data set to NA. Rows are persons and columns are items. The ordinal rating scale is assumed to go from the smallest to largest integer in integer steps unless minRating is specified (see Details). |
|---------|--|
| persons | a numeric vector of person measures with missing values set to NA. The length  |

of persons must equal the number of rows in data.

thresholds a numeric vector of ordered rating category thresholds with no NA. misfit logical for calculating infit and outfit statistics. Default is FALSE.

integer representing the smallest ordinal rating category. Default is NULL (see minRating

Details).

#### **Details**

minRating must be specified if either the smallest or largest possible rating category is not in data (i.e., no person used one of the extreme rating categories). If minRating is specified, the ordinal rating scale is assumed to go from minRating to minRating + length(thresholds) in integer steps.

#### Value

A list whose elements are:

```
item_measures
                  a vector of person measures for each person
item_std_errors
                  a vector of standard errors for the persons
                  if misfit = TRUE, a vector of infit statistics for the items
infit_items
                  if misfit = TRUE, a vector of outfit statistics for the items
outfit_items
```

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## Note

Item measures estimated with ims differ from those estimated with msd because ims assumes all persons use the same rating category thresholds while msd does not. Intended use of ims is with an anchored set of persons and thresholds. Item measures that cannot be estimated will return as NA (e.g., if all responses to an item consist of only the highest rating category, or of only the lowest rating category, that item's item measure cannot be estimated).

# Author(s)

Chris Bradley (cbradley05@gmail.com)

#### See Also

msd

# **Examples**

```
# Simple example with randomly generated values and lowest rating category = 0.
d <- as.numeric(sample(0:4, 500, replace = TRUE))
dm <- matrix(d, nrow = 50, ncol = 10)
pm <- runif(50, -2, 2)
th <- sort(runif(4, -2, 2))
im <- ims(data = dm, persons = pm, thresholds = th, misfit = TRUE, minRating = 0)</pre>
```

misfit

Infit and Outfit Statistics

## **Description**

Calculates infit and outfit statistics for items and persons.

# Usage

```
misfit(data, items, persons, thresholds, minRating = NULL)
```

# Arguments

| data       | a numeric matrix of ordinal rating scale data whose entries are integers with missing data set to NA. Rows are persons and columns are items. The ordinal rating scale is assumed to go from the smallest to largest integer in integer steps unless minRating is specified. |
|------------|--|
| items      | a numeric vector of item measures with missing values set to NA.   |
| persons    | a numeric vector of person measures with missing values set to NA.   |
| thresholds | a numeric vector of ordered rating category thresholds with no NA.   |
| minRating  | integer representing the smallest ordinal rating category. Default is NULL (see  |

Details).

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#### **Details**

minRating must be specified if either the smallest or largest possible rating category is not in data (no person used one of the extreme rating categories). If minRating is specified, the ordinal rating scale is assumed to go from minRating to minRating + length(thresholds).

#### Value

A list whose elements are:

# Author(s)

Chris Bradley (cbradley05@gmail.com)

# **Examples**

```
# Using randomly generated values
d <- as.numeric(sample(0:5, 500, replace = TRUE))
dm <- matrix(d, nrow = 50, ncol = 10)
im <- runif(10, -2, 2)
pm <- runif(50, -2, 2)
th <- sort(runif(5, -2, 2))
m <- misfit(data = dm, items = im, persons = pm, thresholds = th)

# If the lowest or highest rating category is not in \code{data}, specify \code{minRating}
dm[dm == 0] <- NA
m2 <- misfit(data = dm, items = im, persons = pm, thresholds = th, minRating = 0)</pre>
```

msd

Method of Successive Dichotomizations

# **Description**

Estimates item measures, person measures, rating category thresholds and their standard errors using the method of successive dichotomizations. Option provided for anchoring certain items and persons while estimating the rest. Option also provided for estimating infit and outfit statistics.

# Usage

```
msd(data, items = NULL, persons = NULL, misfit = FALSE)
```

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#### **Arguments**

data a numeric matrix of ordinal rating scale data whose entries are integers with missing data set to NA. Rows are persons and columns are items. The ordinal rating scale is assumed to go from the smallest integer to the largest integer in

data in integer steps.

items a numeric vector of anchored item measures. Item measures to be estimated are

set to NA. Default is NULL (see Details).

persons a numeric vector of anchored person measures. Person measures to be estimated

are set to NA. Default is NULL (see Details).

misfit logical for calculating infit and outfit statistics. Default is FALSE.

#### **Details**

items and persons are optional numeric vectors that specify item and person measures that are "anchored" and not estimated. The length of items must equal the number of columns in data and the length of persons must equal the number of rows in data. Only entries set to NA in items and persons are estimated. Default for both items and persons is NULL, which is equivalent to a vector of NA so that all items and persons are estimated.

#### Value

A list whose elements are:

item\_measures a vector of item measures for each item

person\_measures

a vector of person measures for each person

thresholds a vector of average rating category thresholds used by the persons when rating

the items

item\_std\_errors

a vector of standard errors for the items

person\_std\_errors

a vector of standard errors for the persons

threshold\_std\_errors

a vector of standard errors for the thresholds

item\_reliability

reliability of the item measures

person\_reliability

reliability of the person measures

infit\_items if misfit = TRUE, a vector of infit statistics for the items

outfit\_items if misfit = TRUE, a vector of outfit statistics for the items

 $infit\_persons$  if misfit = TRUE, a vector of infit statistics for the persons

outfit\_persons if misfit = TRUE, a vector of outfit statistics for the persons

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#### Note

The axis origin is set by convention at the mean item measure. All item measures and person measures that cannot be estimated will return as NA (e.g., if a person responds with only the highest rating category, or with only the lowest rating category, to all items, that person's person measure cannot be estimated).

The accuracy of msd can be tested using the simdata function (see Examples).

# Author(s)

Chris Bradley (cbradley05@gmail.com)

## References

Bradley, C. and Massof, R. W. (2018) Method of successive dichotomizations: An improved method for estimating measures of latent variables from rating scale data. *PLoS One*, **13(10)** doi:10.1371/journal.pone.0206106

#### See Also

simdata

## **Examples**

```
# Simple example using a randomly generated ratings matrix
d <- as.numeric(sample(0:5, 200, replace = TRUE))</pre>
dm \leftarrow matrix(d, nrow = 20, ncol = 10)
m1 <- msd(dm, misfit = TRUE)</pre>
# Anchor first 5 item measures and first 10 person measures
im <- m1$item_measures</pre>
im[6:length(im)] <- NA</pre>
pm <- m1$person_measures
pm[11:length(pm)] <- NA
m2 <- msd(dm, items = im, persons = pm)</pre>
# To test the accuracy of msd using simdata, set the mean item measure to zero
# (axis origin in msd is the mean item measure) and the mean threshold to
# zero (any non-zero mean threshold is reflected in the person measures).
im <- runif(100, -2, 2)
im <- im - mean(im)</pre>
pm < -runif(100, -2, 2)
th <- sort(runif(5, -2, 2))
th <- th - mean(th)
d <- simdata(im, pm, th, missingProb = 0.15, minRating = 0)</pre>
m \leftarrow msd(d)
# Compare msd parameters to true values. Linear regression should
# yield a slope very close to 1 and an intercept very close to 0.
lm(m$item_measures ~ im)
lm(m$person_measures ~ pm)
lm(m$thresholds ~ th)
```

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msdprob

Rating Category Probabilities

## **Description**

Estimates the probability of observing each rating category given a set of ordered rating category thresholds.

## Usage

```
msdprob(x, thresholds)
```

#### **Arguments**

x a real number or a vector of real numbers with no NA representing a set of

person minus item measures.

thresholds a numeric vector of ordered rating category thresholds with no NA.

#### **Details**

It is assumed that thresholds partitions the real line into length(thresholds)+1 ordered intervals that represent the rating categories.

#### Value

A matrix of probabilities where each of the length(thresholds)+1 rows represents a different rating category (lowest rating category is the top row) and each of the length(x) columns represents a different person minus item measure.

# Note

msdprob can be used to create probability curves, which represent the probability of rating an item with each rating category as a function of the person measure minus item measure (see Examples).

## Author(s)

Chris Bradley (cbradley05@gmail.com)

## **Examples**

```
# Simple example p \leftarrow msdprob(c(1.4, -2.2), thresholds = c(-1.1, -0.3, 0.5, 1.7, 2.2))
# Plot probability curves — each curve represents the probability of # rating an item with a given rating category as a function of the # person measure minus item measure. x \leftarrow seq(-6, 6, 0.1)
p \leftarrow msdprob(x, thresholds = c(-3.2, -1.4, 0.5, 1.7, 3.5))
```

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pms

Person Measures

## **Description**

Estimates person measures assuming item measures are known and all persons use the same set of rating category thresholds.

# Usage

```
pms(data, items, thresholds, misfit = FALSE, minRating = NULL)
```

# **Arguments**

| data       | a numeric matrix of ordinal rating scale data whose entries are integers with missing data set to NA. Rows are persons and columns are items. The ordinal rating scale is assumed to go from the smallest to largest integer in integer steps unless minRating is specified (see Details). |
|------------|--|
| items      | a numeric vector of item measures with missing values set to NA. The length of items must equal the number of columns in data.   |
| thresholds | a numeric vector of ordered rating category thresholds with no NA.   |
| misfit     | logical for calculating infit and outfit statistics. Default is FALSE.   |
| minRating  | integer representing the smallest ordinal rating category. Default is NULL (see Details).  |

# **Details**

minRating must be specified if either the smallest or largest possible rating category is not in data (i.e., no person used one of the extreme rating categories). If minRating is specified, the ordinal rating scale is assumed to go from minRating to minRating + length(thresholds) in integer steps.

#### Value

```
A list whose elements are:

person_measures

a vector of person measures for each person

person_std_errors

a vector of standard errors for the persons

infit_persons if misfit = TRUE, a vector of infit statistics for the persons

outfit_persons if misfit = TRUE, a vector of outfit statistics for the persons
```

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## Note

Person measures estimated with pms differ from those estimated with msd because pms assumes all persons use the same rating category thresholds while msd does not. Intended use of pms is with an anchored set of items and thresholds. Person measures that cannot be estimated will return as NA (e.g., if a person responds to all items with only the highest rating category, or with only the lowest rating category, that person's person measure cannot be estimated).

## Author(s)

Chris Bradley (cbradley05@gmail.com)

#### See Also

msd

# **Examples**

```
# Simple example with randomly generated values and lowest rating category = 0
d <- as.numeric(sample(0:4, 500, replace = TRUE))
dm <- matrix(d, nrow = 25, ncol = 20)
im <- runif(20, -2, 2)
th <- sort(runif(4, -2, 2))
pm <- pms(data = dm, items = im, thresholds = th, misfit = TRUE, minRating = 0)</pre>
```

rasch

Dichotomous Rasch Model

## **Description**

Estimates item measures, person measures and their standard errors using the dichotomous Rasch model. A special case of the function msd when the rating scale consists of only two rating categories: 0 and 1. Option provided for anchoring certain items and persons while estimating the rest. Option also provided for estimating infit and outfit statistics.

#### **Usage**

```
rasch(data, items = NULL, persons = NULL, misfit = FALSE)
```

## **Arguments**

| data    | a numeric matrix of 0's and 1's with missing data set to NA. Rows are persons and columns are items.                        |
|---------|---|
| items   | a numeric vector of anchored item measures. Item measures to be estimated are set to NA. Default is NULL (see Details).     |
| persons | a numeric vector of anchored person measures. Person measures to be estimated are set to NA. Default is NULL (see Details). |
| misfit  | logical for calculating infit and outfit statistics. Default is FALSE.  |

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#### **Details**

items and persons are optional numeric vectors that specify item and person measures that should be "anchored" and not estimated. The length of items must equal the number of columns in data and the length of persons must equal the number of rows in data. Only entries set to NA in items and persons are estimated. Default for both items and persons is NULL, which is equivalent to a vector of NA so that all items and persons are estimated.

#### Value

```
A list whose elements are:
```

```
item_measures a vector of item measures for each item
person_measures
                  a vector of person measures for each person
item_std_errors
                  a vector of standard errors for the items
person_std_errors
                  a vector of standard errors for the persons
item_reliability
                  reliability value for the items
person_reliability
                  reliability value for the persons
infit_items
                  if misfit = TRUE, a vector of infit statistics for the items
outfit_items
                  if misfit = TRUE, a vector of outfit statistics for the items
infit_persons
                  if misfit = TRUE, a vector of infit statistics for the persons
outfit_persons if misfit = TRUE, a vector of outfit statistics for the persons
```

#### Note

The axis origin is set by convention at the mean item measure. All item measures and person measures that cannot be estimated will return as NA (e.g., if a person responds with a single rating category to all items, that person's person measure cannot be estimated).

rasch is the basis for the "successive dichotomizations" in msd and is repeatedly called by msd when there are three or more rating categories.

The accuracy of rasch can be tested using the simdata function (see Examples).

## Author(s)

Chris Bradley (cbradley05@gmail.com)

#### See Also

msd simdata

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## **Examples**

```
# Simple example using a randomly generated ratings matrix
d <- as.numeric(sample(0:1, 200, replace = TRUE))</pre>
dm \leftarrow matrix(d, nrow = 20, ncol = 10)
m1 <- rasch(dm, misfit = TRUE)</pre>
# Anchor first 5 item measures and first 10 person measures
im <- m1$item_measures</pre>
im[6:length(im)] <- NA</pre>
pm <- m1$person_measures
pm[11:length(pm)] <- NA</pre>
m2 <- rasch(dm, items = im, persons = pm)</pre>
# To test the accuracy of rasch using simdata, set the true mean item measure to
# zero (axis origin in rasch is the mean item measure). Note that the threshold for
# dichotomous data is at 0.
im < -runif(100, -2, 2)
im <- im - mean(im)</pre>
pm <- runif(100, -2, 2)
th <- 0
d <- simdata(im, pm, th, missingProb = 0.15, minRating = 0)</pre>
m <- rasch(d)
# Compare rasch parameters to true values. Linear regression should
# yield a slope very close to 1 and an intercept very close to 0.
lm(m$item_measures ~ im)
lm(m$person_measures ~ pm)
```

simdata

Simulated Rating Scale Data

## **Description**

Generates simulated rating scale data given item measures, person measures and rating category thresholds.

# Usage

```
simdata(items, persons, thresholds, missingProb = 0, minRating = 0)
```

tails).

# **Arguments**

items a numeric vector of item measures with no NA.

persons a numeric vector of person measures with no NA.

thresholds a numeric vector of ordered rating category thresholds with no NA.

missingProb a number between 0 and 1 specifying the probability of missing data.

minRating integer representing the smallest ordinal rating category. Default is 0 (see De-

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#### **Details**

It is assumed that the set of ordinal rating categories consists of all integers from the lowest rating category specified by minRating to the highest rating category, which is minRating + length(thresholds).

#### Value

A numeric matrix of simulated rating scale data.

## Note

simdata can be used to test the accuracy of msd (see Examples).

#### Author(s)

Chris Bradley (cbradley05@gmail.com)

## See Also

msd

## **Examples**

```
# Use simdata to test the accuracy of msd. First, randomly generate item
# measures, person measures and thresholds with 15 percent missing data and
# ordinal rating categories from 0 to 5. Then, set mean item measure to zero
# (axis origin in msd is the mean item measure) and mean threshold to zero
# (any non-zero mean threshold is reflected in the person measures).
im <- runif(100, -2, 2)
pm <- runif(100, -2, 2)
th <- sort(runif(5, -2, 2))
im <- im - mean(im)</pre>
th <- th - mean(th)
d <- simdata(im, pm, th, missingProb = 0.15, minRating = 0)</pre>
m \leftarrow msd(d)
# Compare msd parameters to true values. Linear regression should
\# yield a slope very close to 1 and an intercept very close to 0.
lm(m\$item\_measures \sim im)
lm(m$person_measures ~ pm)
lm(m$thresholds ~ th)
```

thresh

Rating Category Thresholds

## **Description**

Estimates rating category thresholds for msd given rating scale data, item measures and person measures.

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## Usage

```
thresh(data, items, persons)
```

# **Arguments**

data a numeric matrix of ordinal rating scale data whose entries are integers with

missing data set to NA. Rows are persons and columns are items. The ordinal rating scale is assumed to go from the smallest integer to the largest integer in

data in integer steps.

items a numeric vector of item measures with missing values set to NA (see Details).

persons a numeric vector of person measures with missing values set to NA (see Details).

#### **Details**

The length of items must equal the number of columns in data and the length of persons must equal the number of rows in data. Neither items nor persons can consist of only NA.

#### Value

A list whose elements are:

thresholds a vector of average rating category thresholds used by the persons when rating the items

threshold\_std\_errors

a vector of standard errors for the thresholds

# Note

thresh is a special case of msd when item measures and person measures are known.

#### Author(s)

Chris Bradley (cbradley05@gmail.com)

# See Also

msd

# **Examples**

```
# Using randomly generated values
d <- as.numeric(sample(0:5, 1000, replace = TRUE))
m <- matrix(d, nrow = 50, ncol = 20)
im <- runif(20, -2, 2)
pm <- runif(50, -2, 2)
th1 <- thresh(m, items = im, persons = pm)

# Anchor first 10 item measures and first 10 person measures
im[11:length(im)] <- NA
pm[11:length(pm)] <- NA
th2 <- thresh(m, items = im, persons = pm)</pre>
```

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